

# Simple model for urban traffic between two signalized intersections

Jan Příklad

Department of Adaptive Systems  
Institute of Information Theory and Automation  
Academy of Sciences of the Czech Republic

Seminář oddělení AS  
November 26, 2012

# Outline

- 1 Introduction
- 2 Motivation
- 3 Original model
- 4 Piecewise Linear Model
- 5 Experiment

# Motivation

## Move from HŘSD

HŘSD  $\Rightarrow$  NOMŘÍZ: Better sampling, better information about model

Current status:

- Model updated for sampling interval 5-10 s
- Waiting for the new version of micro-simulator
- Industrial partner questions the need for high sampling rate

## HŘSD

## Macro-level model – queue equation

## Queue development

$$\xi_{i,k+1} = \delta_{i,k}\xi_{i,k} + (\delta_{i,k}S_i + (1 - \delta_{i,k})l_{in,i,k})z_{i,k} + l_{in,i,k}$$

$\xi \dots$  queue length,  $\delta \dots$  saturation flag,  $\delta \in \{0, 1\}$ ,  $z \dots$  relative green length

Equation **assumes uniform arrivals** – works well for boundary nodes, too simple for interior nodes.

Upstream intersections significantly influence arrival traffic flow.

# NOMŘÍZ

## The proposed model

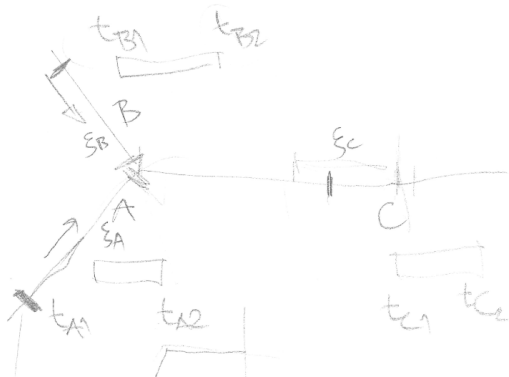
Vehicle movements in the real world are quite complex and difficult to model.

We will simplify the behaviour of vehicles to the maximum possible extent

- we will not take into account acceleration and deceleration
- we will classify the movements of vehicles into two classes:
  - ① stopped vehicle, waiting in a queue, and
  - ② vehicle moving with a constant speed of passage  $v$ .

# Building the model

## Basic building block



# Building the model

## Basic building block

Basic building block of the system is a simple ramp function defined by its vector of parameters  $\theta = (x_1, x_2, y_1, y_2)$  as

$$\begin{aligned} \rho(x, \theta) &= \rho(x, x_1, x_2, y_1, y_2) = \\ &= \begin{cases} y_1 & \text{if } x \leq x_1 \\ y_1 + (x - x_1) \frac{y_2 - y_1}{x_2 - x_1} & \text{if } x_1 < x < x_2 \\ y_2 & \text{if } x \geq x_2 \end{cases} \end{aligned}$$

# Building the model

## Computing capacity

Given a signal plan timing, capacity  $c_{i,l}$  of a lane  $l$  at intersection  $i$  can be then computed as

$$c_{i,l}(t) = \rho(t, t_{\text{on},i,l}, t_{\text{off},i,l}, 0, \frac{S_{i,l}}{3600})$$

where  $t_{\text{on},i,l}$  and  $t_{\text{off},i,l}$  denote beginning and end time of the green signal in the signal plan cycle in seconds, and  $S_{i,l}$  stands for the saturation flow of the lane in vehicles per hour.



# Building the model

## Demand function at the boundary

The cumulative demand volume  $d_{i,l}(t)$  may be described in a similar manner for all incoming lanes of an intersection that is situated on the boundary:

$$d_{i,l}(t) = \rho(t, 0, T_c, 0, D_{i,l}).$$

Here,  $T_c$  is the signal plan cycle length and  $D_{i,l}$  is the count of vehicles arriving during that cycle from the outside.

# Building the model

## Demand function at the boundary

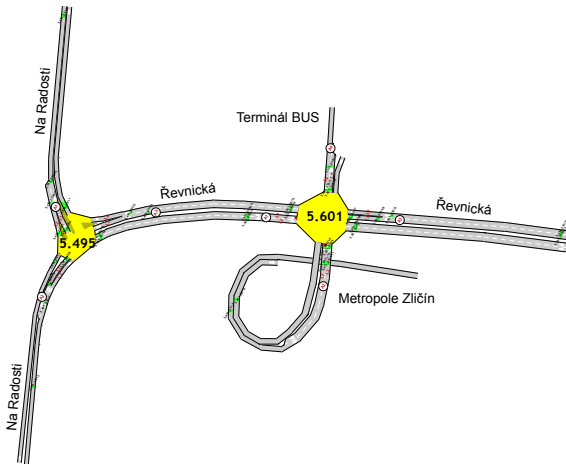
For all downstream intersections, the demand volume is given as a sum of several ramp functions which define partial volumes arriving from all possible lanes of their upstream intersections  $\mathcal{U}_{i,l}$ :

$$d_{i,l}(t) = \sum_{j,n \in \mathcal{U}_{i,l}} v_{j,n}(t).$$

$$c = \sum_{i \in L} \rho(t_{\text{on},i}, t_{\text{off},i}, S_i)$$

# Experiment

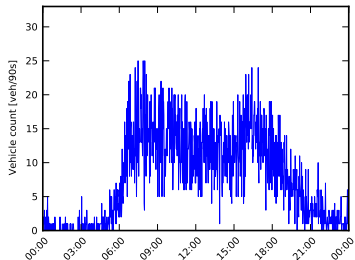
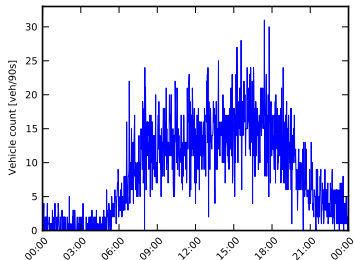
## One lane on Zličín



# Experiment

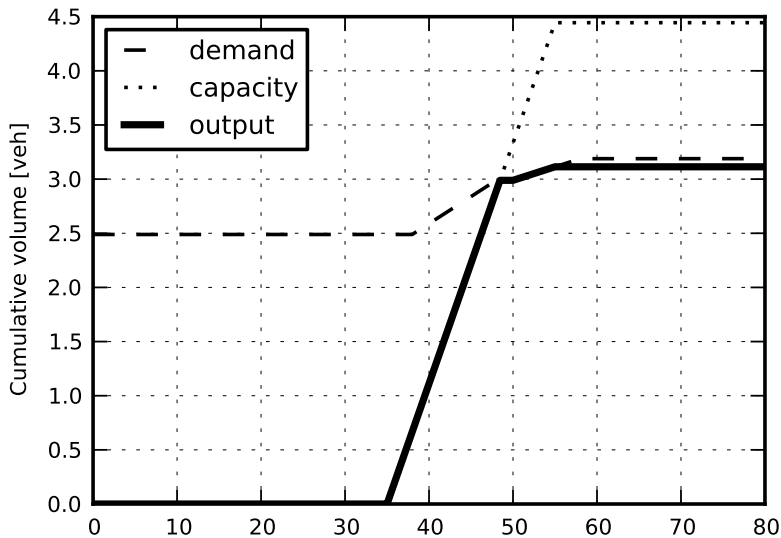
## One lane on Zličín

### Input flows (2007 data)



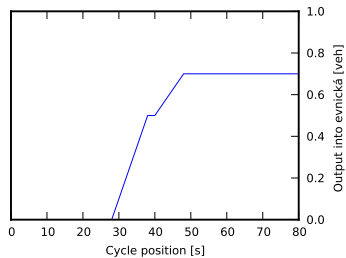
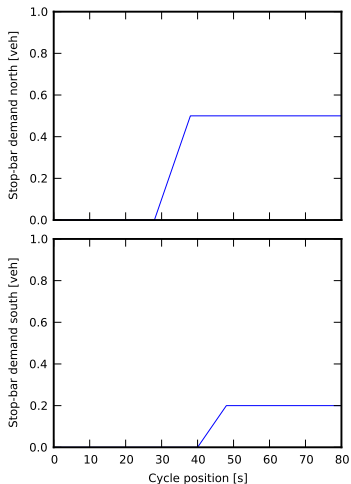
# Experiment

## Composition of the queue at C



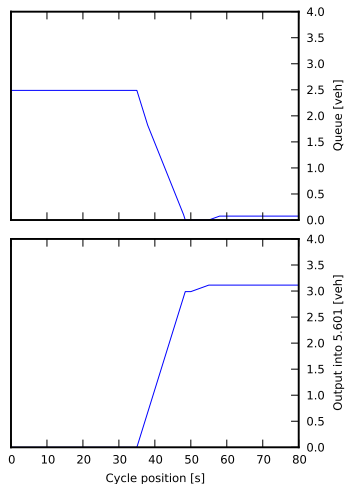
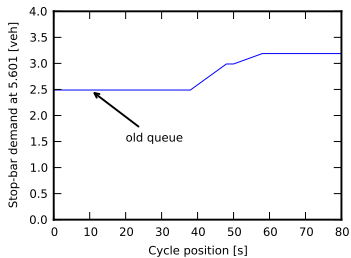
# Experiment

## Inputs



# Experiment

## Outputs



# Further work

## Thorough simulation

Better arrival models

Cycle reaching over  $T_c$ , i.e.  $t_1 > t_2$

Quantisation of vehicle output – only integers allowed (russian roulette?)

Extension to multi-lane approach

## Filtration based on measurements

## Control synthesis